

PART B — (5 × 16 = 80 marks)

11. (a) Discuss the following methods to solve the given differential equation :

$$EI \frac{d^2 y}{dx^2} - M(x) = 0$$

with the boundary conditions $y(0) = 0$ and $y(H) = 0$

- (i) Variational method
(ii) Collocation method.

Or

- (b) For the spring system shown in Figure 1, calculate the global stiffness matrix, displacements of nodes 2 and 3, the reaction forces at node 1 and 4. Also calculate the forces in the spring 2. Assume, $k_1 = k_3 = 100$ N/m, $k_2 = 200$ N/m, $u_1 = u_4 = 0$ and $P = 500$ N.

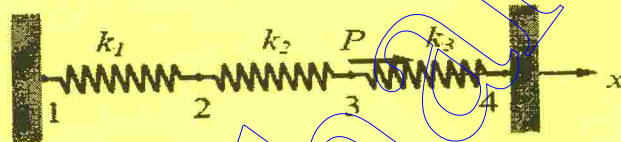


Figure 1 Spring System Assembly

12. (a) Determine the joint displacements, the joint reactions, element forces and element stresses of the given truss elements.

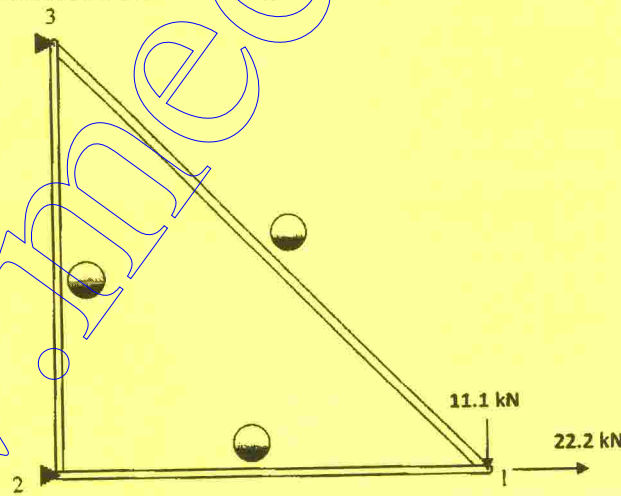


Figure 2 Truss with applied load

Table 1 : Element Property Data

Element	A cm ²	E N/m ²	L m	Global Node Connection	α Degree
1	32.2	6.9e10	2.54	2 to 3	90
2	38.7	20.7e10	2.54	2 to 1	0
3	25.8	20.7e10	3.59	1 to 3	135

Or

- (b) Derive the interpolation function for the one dimensional linear element with a length 'L' and two nodes, one at each end, designated as 'i' and 'j'. Assume the origin of the coordinate system is to the left of node 'i'.

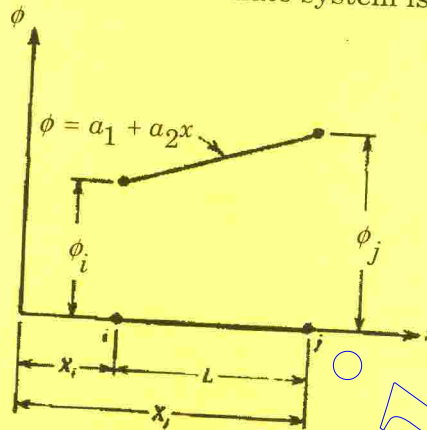


Figure 3 the one-dimensional linear element

13. (a) Determine three points on the 50°C contour line for the rectangular element shown in the Figure 4. The nodal values are $\Phi_i = 42^\circ\text{C}$, $\Phi_j = 54^\circ\text{C}$, $\Phi_k = 56^\circ\text{C}$ and $\Phi_m = 46^\circ\text{C}$.

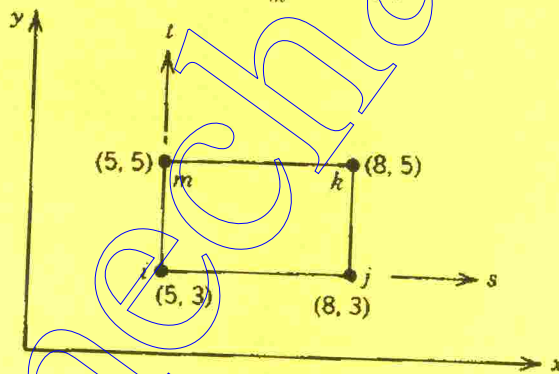


Figure 4 Nodal coordinates of the rectangular element

Or

- (b) The simply supported beam shown in Figure 5 is subjected to a uniform transverse load, as shown. Using two equal-length elements and work-equivalent nodal loads obtain a finite element solution for the deflection at mid-span and compare it to the solution given by elementary beam theory.

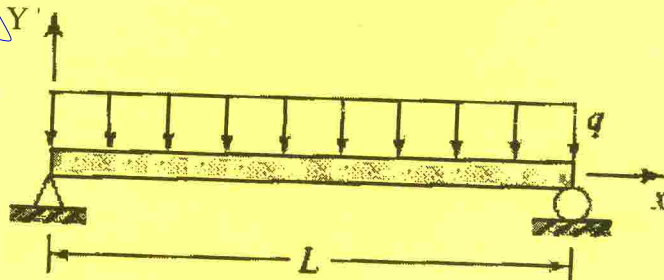


Figure 5 uniformly loaded beam

14. (a) For the plane strain element shown in the Figure 6, the nodal displacements are given as : $u_1 = 0.005$ mm, $u_2 = 0.002$ mm, $u_3 = 0.0$ mm, $u_4 = 0.0$ mm, $u_5 = 0.004$ mm, $u_6 = 0.0$ mm. Determine the element stresses. Take $E = 200$ Gpa and $\gamma = 0.3$. Use unit thickness for plane strain.

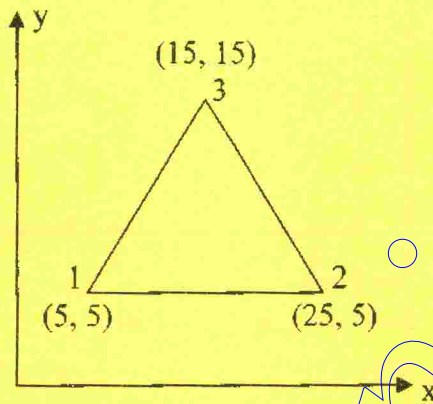


Figure 6 Triangular Element
Or

- (b) Determine the element stiffness matrix and the thermal load vector for the plane stress element shown in Figure 7. The element experiences 20°C increase in temperature. Take $E = 15 \times 10^6$ N/cm², $\gamma = 0.25$, $t = 0.5$ cm and $\alpha = 6 \times 10^{-6}/^\circ\text{C}$.

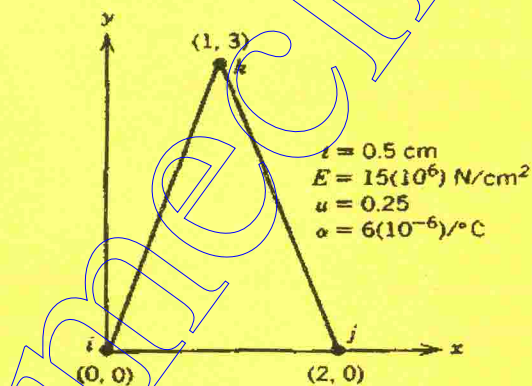


Figure 7 Triangular elastic elements

15. (a) Use Gaussian quadrature to obtain an exact value of the integral.

$$I = \int_{-1}^1 \int_{-1}^1 (r^3 - 1)(s - 1)^2 dr ds.$$

Or

- (b) Define the following terms with suitable examples :

- (i) Plane stress, Plane strain
- (ii) Node, Element and Shape functions
- (iii) Iso-parametric element
- (iv) Axisymmetric analysis.